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Characterization of Fe<sub>3</sub>O<sub>4</sub> nanoparticles for liquid phase immunoassay using brownian relaxation time and magnetic susceptibility

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# Abstract

This article describes the detail characterization of the magnetic properties of magnetic markers (Fe<sub>3</sub>O<sub>4</sub>) in solution for biosensor application. Frequency dependence of the AC susceptibility and the magnetization curve, which were dominated by the Brownian rotation of the marker, Brownian relaxation time were measured. The effect of the viscosity of the carrier liquid on the AC susceptibility was also clarified. The experimental results were analyzed by the singular value decomposition (SVD) method. The distribution of marker size *d* was obtained from the frequency dependence of the AC susceptibility. The distribution of magnetic moment *m* was obtained from the magnetization curve. The relationship between *m* and *d* was also discussed. The present estimation method using SVD technique will be useful to obtain the distribution of particle size *d* and magnetic moment *m*, which are the important parameters of the magnetic marker for biomedical application. We also obtained result, we could classify the particles into three types: Type-I particles with very small *m* and very short  $\tau_N$ , Type-II particles with medium values of *m* and  $\tau_N$ , and Type-III particles with large *m* and very long  $\tau_N$ .

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#### Introduction

Magnetic markers, which are composed of polymercoated magnetic nanoparticles, have been extensively studied for use in biological applications such as cell separation, immunoassays, hyperthermia, and drug delivery. Immunoassays are used to detect biological targets such as disease-related proteins and cells. Magnetic immunoassay techniques that utilize magnetic markers have recently been developed. One of the advantages of this magnetic method is that we can perform immunoassays in the liquid phase; that is, we can magnetically distinguish bound markers from unbound (free) markers. This function can be utilized to eliminate the time-consuming washing process used to separate the two types of markers, i.e., the so-called bound/free separation [1, 2, 3].

This function can be realized by utilizing the Brownian relaxation of magnetic markers in the solution. The difference in the Brownian relaxation time between the bound and free markers can be exploited for the use in liquid-phase immunoassays. For this purpose, several methods have been proposed to prolong the relaxation time of the bound markers. The resulting difference between the magnetic properties of the bound and free markers has been detected using relaxation or susceptibility measurement. [4, 5, 6].

When we apply the Brownian relaxation method for the liquid phase immunoassay, the hydrodynamic diameter  $d_{h}$ , magnetic moment  $m_{B}$ , and anisotropy energy  $E_{\rm B}$  are the key parameters of a magnetic marker because they determine the performance of the magnetic immunoassay. The hydrodynamic diameter  $d_h$  determines the Brownian relaxation time  $\tau_{\rm B}$ , and the magnetic moment  $m_{\rm B}$  determines the signal detected from the markers. The anisotropy energy  $E_{\rm B}$  determines the Neel relaxation time $\tau_{\rm N}$ , which must be much longer than  $\tau_{\mathbf{B}}$ . Therefore, it is necessary to quantitatively evaluate these parameters for practical markers.[18] However, it must be noted that practical markers are usually composed of aggregated magnetic particles. As a result, their magnetic behavior will be different from those

expected from single-domain nanoparticles. These points have not yet been clarified quantitatively. [4, 11, 17].

### **Experimental results**

#### Experimental setup and sample

In this experiment, we used commercial magnetic markers supplied from Ocean Nanotech Company, USA. The marker composed of polymer coated  $Fe_3O_4$  particles, whose specific diameter was 50 nm, and was dispersed in solution with concentration of 5 mg/ml. The 2 µl of the marker solution was diluted by 73 µl of the solution that consisted of the mixture of water and glycerol.

The concentration of the glycerol was changed from 0% to 75% in order to change the viscosity of the solution. In Figure1, an experimental setup is schematically shown. The excitation field of H = Hasin2nft was applied by an excitation coil. A diskshaped sample plate which contained 60  $\mu$ l of the marker solution in its well was used. The size of the well was 5 mm in diameter. The sample plate was rotated by an ultrasonic motor and was positioned under the excitation coil. In this case, the markers were magnetized and had a magnetic moment m. The signal field Bs generated by m was detected by a magneto-resistive (MR) sensor (Honeywell, USA) that was installed 2 mm under the sample plate. The output signal of the MR sensor was connected to the lock-in amplifier in order to obtain both the real and imaginary parts of the signal. [19, 20].

#### AC susceptibility

#### Frequency dependences

Measurements of the frequency dependence of the AC susceptibility are shown in Figure 2. The real part  $\chi'$  and the imaginary part  $\chi''$  are shown in Figurers. 2(a) and 2(b), respectively. As shown, the real part  $\chi'$  decreased monotonically with frequency. On the other hand, the imaginary part  $\chi''$  had a peak value at some frequency: we define the frequency, which gives the maximum value of  $\chi''$  by  $f_p$ . It is well known that this peak frequency is related to the Brownian relaxation time  $\tau_B$  of the marker as  $f_p = 1/(2\pi\tau_B)$ .

Sample	1	2	3	4	5	6
Water (%)	100	85	70	55	40	25
Glycerol (%)	0	15	30	45	60	75
f <sub>p</sub> (Hz)	2500	1750	1000	390	120	70
Viscosity	1	1.4	2.5	6.4	21	36

**Table 1.** Samples with different concentration of glycerol. Viscosity of the mixed solution was normalized by that of pure water (sample 1).

The peak frequencies  $f_p$  significantly changed among samples. They were approximately 2500, 1750, 1000, 390, 120 and 70 Hz for the samples 1 to 6, respectively. This large change of  $f_p$  was due to the difference in the viscosity of the carrier liquid, as will be shown below. [19, 21].

# Effect of different viscosity liquid

As shown in Figure 2 (b), the peak frequency became lower from sample 1 to 6. As listed in Table 1, this corresponds to the increase of the glycerol concentration in the solution. Since the viscosity of the glycerol is much higher than that of the water, the viscosity of the mixed solution becomes higher with the increase of the glycerol concentration. The effective viscosity of the mixed solution can be obtained as follows.



Fig. 1. Block diagram of the experimental set up.

It is well known that the Brownian relaxation time is given by  $\tau_B = 3\eta V_h/k_B T$ , where  $\eta$  is the viscosity of the liquid;  $V_h$  is the hydrodynamic volume of the particle. Therefore, the peak frequency  $f_p$  is inversely proportional to the viscosity  $\eta$ . using the measured value of  $f_p$  listed in Table 1, we can estimate the viscosity of each sample. In Figure 3, viscosity of samples, which was normalized by that of pure water

(sample 1), was shown as a function of the concentration ratio of glycerol. As shown, viscosity of the mixed solution became 1.4, 2.5, 6.4, 21 and 36 times larger than that of water (sample 1) for samples 2 to 6. [21].

### Analysis

#### Expression for susceptibility and magnetization

We analyze the experimental results shown in this section by taking account of the distribution of size d and magnetic moment m of the marker. In this case, we define the parameters as follow. The diameter of the i - th magnetic nanoparticle is  $d_{mi}$ , thickness of the coating material is t, and the hydrodynamic diameter of the marker is  $d_{hi} = d_{mi} + 2t$ . Distribution function of the diameter is  $f(d_h)$ . then, the number of i - th markers is  $n_i = f_i(d_{hi})\Delta d_{hi}$ , and the magnetic moment is given by  $m_i = \mu_0 M_s V_{mi}$  where  $V_{mi} = (\pi/6)d_{mi}^3$  is the volume of the magnetic nanoparticle and  $M_s$  is the saturation magnetization.

When a small AC field is applied, the real and imaginary parts of the susceptibility are given by [12, 13],

$$\chi'(\omega) = \frac{1}{3\mu_0 k_{\rm B} T V_{\rm T}} \sum_i \frac{n_i m_i^2}{1 + (\omega \tau_i)^2} + \chi_{\infty}$$
(1)

$$\chi''(\omega) = \frac{1}{3\mu_0 k_{\rm B} T V_{\rm T}} \sum_i \frac{\omega \tau_i n_i m_i^2}{1 + (\omega \tau_i)^2}$$
(2)

where  $k_B$  is the Boltzmann constant,  $V_T = \sum n_i m_i^2$  is the total volume of the sample, and  $\chi_{\infty}$  represents the susceptibility at high frequency limit. The relaxation time of the Brownian rotation of the particle is given by  $\tau_i = \frac{3\eta V_{h1}}{k_B T}$ .



**Fig. 2.** Frequency dependence of the AC susceptibility for 6 samples listed in Table 1. (a) Real part  $\chi'$ , and (b) imaginary part  $\chi''$ .

# Basic Theory of MNP and Particle Size Measurement Numerical model used to measure particle size distribution

The nanoscale thermal motion and surface energy of MNPs, and their interaction with magnetic fields, obey the universal rules of statistical physics. The magnetization curve is obtained as a result of the combined action of magnetic fields and thermal motion. For a multi-size distribution system of *noninteracting* particles, the average magnetization is [13, 14, 15, 20].



**Fig. 3.** Viscosity of the water/glycerol mixed solution as a function of glycerol concentration.

$$M(H) = \int \mu_0 M_d L(D, H) \frac{\pi D^3}{6} f(D) dD$$
(3)

with  $L(D, H) = L(\xi) = \operatorname{coth} \xi - \frac{1}{\xi}$  (4)

$$\xi = \frac{\mu_0 M_d \frac{\pi}{6} D^2 H}{k_{\rm B} T} \tag{5}$$

where L denotes the Langevin function, D denotes the MNP diameter, f is the particle size distribution function,  $M_d$  is the saturation magnetization and H is the strength of the external magnetizing field. Magnetic moment information can be obtained using SQUID, VSM, or atomic force microscopy.

If the particle diameter **D** and magnetic field  $H_i$  are both given discrete values, the magnetization equation then becomes [14, 15],

$$M(H_i) = \sum_{j=1}^{N} \mu_0 M_{d_i} \frac{\pi}{6} D_j^2 L\left(\frac{\mu_0 M_{d_k}^* D_j^* H_i}{k_0 T}\right) f(D_j) \Delta D_j \quad , i = 1, \dots, Z$$
(6)

where *N* denotes the number of sampling points used for the particle diameter and *Z* represents the sampling steps used for the magnetizing field  $H_i$ . Thus, the magnetic moment matrix *M* can be rewritten as,

$$M(H_i) = A(i, j)f(D_j)$$
 or  $M(i) = A(i, j)f(j)$  with  
 $A(i, j) = \mu_0 M_d \frac{\pi}{6} D_j^{T} L\left(\frac{\mu_0 M_d \frac{\pi}{6} D_j^{T} H_j}{k_T}\right) \Delta D_j$ ,  $i = 1 \dots Z$ ,  $j = 1 \dots N$  (7)

The magnetic properties of the MNPs can be described using a numerical matrix equation of the following form

$$M(i) = A(i, j)f(j)$$
(8)

where A(i, j) may be determined directly by the

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magnetic physics of the MNP magnetization, M(i) represents the magnetic curve and f (j) is the particle size distribution function. Details of this discretization and its effects on the ill-condition of the matrix equation, as well as a discussion of the range of particle sizes and magnetization fields used in the analysis.



**Fig. 4.** Frequency dependence of the susceptibility. (a) sample 1, (b) sample 4, and (c) sample 6. The solid lines are calculated from Eqs. (1) and (2) by using the size distribution shown in Figure 5 the symbols are experimental results.

All the terms in equation (6) are non-negative. Because the particle size distribution function f (j) is the only unknown term, the estimation of particle size distribution may be reduced to the solution of a nonnegative matrix equation.



**Fig. 5.** Size distribution for the different mixed solution with water and glycerol.



**Fig. 6.** Dependence of  $M_1(0)$  on  $H_a$ . Circles represent the experimental results, while solid line represents the result calculated from eq. (9) using the estimated magnetic moment distribution shown in Figure 7. Eqs. (3)– (8) shows that the size distribution of a super-paramagnetic MNP system, whose magnetization is described by the Langevin equation, may be estimated using the methods presented herein, regardless of whether a water based or oilbased MNP is used. This model is the Numerical model used to measure particle size distribution.

In the study described herein, we obtained the detail method used to estimate the size distribution of the MNPs from the frequency dependence of AC susceptibility by SVD method [19, 20].

## $M ext{-}H$ Curve

In our experiment, we measured the magnetization of the markers in solution. In Figure. 6, the circles show the experimental results. Here, vertical axis represents the value of magnetization  $M_1$  at f = 0 Hz,  $M_1(0)$ , while the horizontal axis represents the amplitude  $H_a$  of the excitation field. In the experiment, the value of  $M_1(0)$  was obtained from the value of  $M_1(90 \text{ Hz})$  since  $M_1$  became constant independent of the frequency at low frequencies.



**Fig.** 7. Estimated distribution of magnetic moment of the markers. (a)  $g_i - m_i$  curve and (b)  $g_i m_i^2 - m_i$  curve.

As shown,  $M_1$  increased linearly at small values of  $H_a$ , while it began to saturate at higher  $H_a$ . It is known that this saturation of M was caused by the nonlinear effect of Brownian relaxation in high excitation fields. Expression for the  $M_1$ -H curve is given by [14, 15]

$$M_{1}(0) = \frac{H}{3\mu_{0}k_{B}TV_{T}} \sum_{i} g_{i}(m_{i})m_{i}^{2} \left[\frac{\chi_{i}(0)}{\chi_{0}}\right] \Delta m_{i} \approx \frac{H}{3\mu_{0}k_{B}TV_{T}} \sum_{i} g_{i}m_{i}^{2} \left(1 - \frac{\xi_{i}^{3}}{10 + 9\xi_{i} + 3.81\xi_{i}^{2} + \xi_{i}^{3}}\right) \Delta m_{i}$$
(9)

where  $g_i(m_i)$  is the distribution function of m, and

$$\xi_i = m_i H / k_R T \tag{10}$$

is the parameter representing the strength of the applied field. The relationship between the distribution function  $f(d_h)$  and g(m) is given as

follows. Note that  $g_i \Delta m_i$  is the number of particles with the magnetic moment  $m_i$ , while  $f_i \Delta d_{hi}$  is the number of particles with diameter  $d_{hi}$ . Since these values should be the same, we obtain

$$f(d)\Delta d = g(m)\Delta m \tag{11}$$

### Singular Value Decomposition Method (SVD)

SVD has been used to detect and characterize structural intermediates in biomolecular small-angle scattering experiments (Chen et al., 1996). This study provides a good illustration of how SVD can be used to extract biologically meaningful signals from the data. Small-angle scattering data were obtained from partially unfolded solutions of lysozyme, each consisting of a different mix of folded, collapsed and unfolded states. The data for each sample was in the form of intensity values sampled at on the order of 100 different scattering angles. UV spectroscopy was used to determine the relative amounts of folded, collapsed and unfolded lysozyme in each sample. SVD was used in combination with the spectroscopic data to extract a scattering curve for the collapsed state of the lysozyme, a structural intermediate that was not observed in isolation.



**Fig. 8.** Estimated size dependences of magnetic moment *m*. The results were obtained by combining the  $n_i m_i^2 - d_{hi}$  curve shown in Figure. 5 and the  $g_i m_i^2 - m_i$  curve shown in Figure 7 (b).

In this work, we apply the SVD method for the calculation of size distribution of the practical marker. Since the frequency dependence of the susceptibility is theoretically given by Eqs. (1) and (2), we can estimate the size distribution of the markers by comparing the experimental results with the

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theoretical ones, as shown below. In the comparison, we first choose N sets of  $\tau_i$  (i = 1, ..., N) in Eqs. (1) and (2).

Then we take  $n_i m_i^2$  as unknown values, and determine the values of  $n_i m_i^2$  so as to obtain the best fit between the experimental and theoretical results. With this technique we can obtain the  $\tau_i - n_i m_i^2$  curve. This curve is transformed in to the  $d_{hi} - n_i m_i^2$  curve using Eq. (1), which gives the size distribution of the markers.



**Fig. 9.** Frequency dependence of real part of the AC susceptibility.  $\chi'_{sus}$  and  $\chi'_{imm}$  represents the real part of the susceptibilities in suspension and immobilized cases, respectively.

To determine the values of *nimi*<sup>2</sup> in the presence of experimental error in the practical data, we use the mathematical technique known as SVD method. Details of the SVD methods are described in refs [16, 17].

### Magnetic moment

### Distribution of Magnetic Moment m

Next, we estimate the distribution of magnetic moment *m* from the magnetization curve shown in Figure 6. For this purpose, we compare the experimental results with Eq. (9). In this case, we first choose *N* sets of  $m_i$  (i = 1,... N) in Eq. (9). Then we take  $g_i$  as unknown values, and determine the values so as to obtain the best fit between the experimental and theoretical results by using the SVD method.

In Figure 7 (a), the estimated distribution of m, i.e.,  $g_i$ - $m_i$  curve is shown. As shown, the value of m distributed from  $5x10^{-25}$  to  $5x10^{-24}$  Wbm with mean value of  $m=3x10^{-24}$  Wbm. For the following discussion, we also show in Figure 7 (b) the  $g_im_i^2-m_i$  curve. Substituting the distribution of m shown in Figure 7 (a) into Eq. (9), we could reconstruct the M-H curve. In Figure 6, the solid line shows the reconstructed results. As shown, good agreement was obtained between the experimental and reconstructed results. This agreement indicates the validity of the estimation of m distribution.



**Fig. 10.** M-H curve in weak magnetic field.  $M_{sus}$  and  $M_{imm}$  represent the magnetizations in suspension and immobilized cases, respectively.

#### Relationship between m and d

We now discuss the relationship between the magnetic moment m and size d. In the case of single domain particles, it is well known that m is proportional to the volume of the particle, i.e., m is proportional to  $d^3$ .

In practical markers, however, aggregation of particles occurs in making markers. Therefore, it is expected that the magnetic marker consisted of agglomerate of particles. In this case, the magnetic moments of individual particles within the agglomerate should not align in the same direction, i.e., agglomerate of particles will behave like multi-domain particles. As a result, simple relationship that m is proportional to  $d^3$  should be modified in this case.

The relationship between m and d can be obtained by combining the  $n_im_i^2-d_{hi}$  curve shown in Figure 5 and the  $g_im_i^2-m_i$  curve shown in Figure 7 (b). In Figure 8, circles represent the estimated dependence of m on d. As shown, m increased in proportion to the  $d^3$  for the case of d < 40 nm. This relationship is consistent with the result of single domain particles. When d becomes larger, on the other hand, dependence of m on dchanged: m becomes proportional to  $d^2$ , and then proportional to d with the increase of d. It must be noted that Fe<sub>3</sub>O<sub>4</sub> is expected to form the single domain particle when the diameter d is less than 40 nm, while it forms the multi-domain particle for the case of d > 40 nm. The result shown in Figure 8 is consistent with this prediction.

We have also measured the frequency dependence of the real part of the AC susceptibility  $(\chi')$  and magnetization (M-H) curves of different commercial markers. Examples are shown in Figure. 9 and Figure. 10, where both results for suspension and immobilized samples are shown. Analyzing these data, we can obtain the parameters of the markers, such as hydrodynamic diameter  $d_h$ , magnetic moment *m*, and anisotropy energy  $E_{\rm B}$  [22]. In Type-I markers, magnetic interaction is negligible, and hence they have small values of m and  $E_{\rm B}$  (or short Neel relaxation time  $\tau_N$ ). In Type-II markers, magnetic interaction is medium, and hence they have large m and medium  $E_{\rm B}$  (or medium  $\tau_{\rm N}$ ). In Type-III markers, magnetic interaction is strong, and hence they have large *m* and  $E_B$  (or long  $\tau_N$ ). As shown in Figure 9, we can estimate the contribution of each type of markers to the susceptibility signal. Type III markers give the difference in the susceptibility between the suspension  $(\chi'_{sus})$  and immobilized  $(\chi'_{imm})$  cases. Contribution of Type II and Type I markers can be estimated by the susceptibility in low and high frequency region of the immobilized sample, respectively. Similarly, in Figure 10, type III markers give the difference in the magnetization between the suspension  $(M_{sus})$  and immobilized  $(M_{imm})$  cases. Nonlinearity of *M*-*H* curve of the immobilized case in weak field is dominated by the Type II markers. Since Type-III makers contribute to the signal in liquidphase immunoassays using Brownian relaxation, it is important to choose a sample having a large portion of Type-III markers.

#### Conclusions

We have characterized the magnetic properties of magnetic markers in solution for biosensor application. Frequency dependence of the AC susceptibility and the magnetization curve, which were dominated by the Brownian rotation of the marker, were measured. The effect of the viscosity of the carrier liquid on the AC susceptibility was also clarified. The experimental results were analyzed by the singular value decomposition (SVD) method.

The distribution of marker size d was obtained from the frequency dependence of the susceptibility. The distribution of magnetic moment m was obtained from the magnetization curve. The relationship between m and d was also discussed. The present estimation method using SVD technique will be useful to obtain the distribution of d and m, which are the important parameters of the magnetic marker for biosensor application.

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# Declaration

All the authors do not have any possible conflicts of interest.

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